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Verification within Complexity: Comparing Spatial Fields

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National Center for Atmospheric Research

Forecasting from Complexity Workshop

Institute for Mathematics and its Applications (IMA)

Wednesday, 25 April 2018

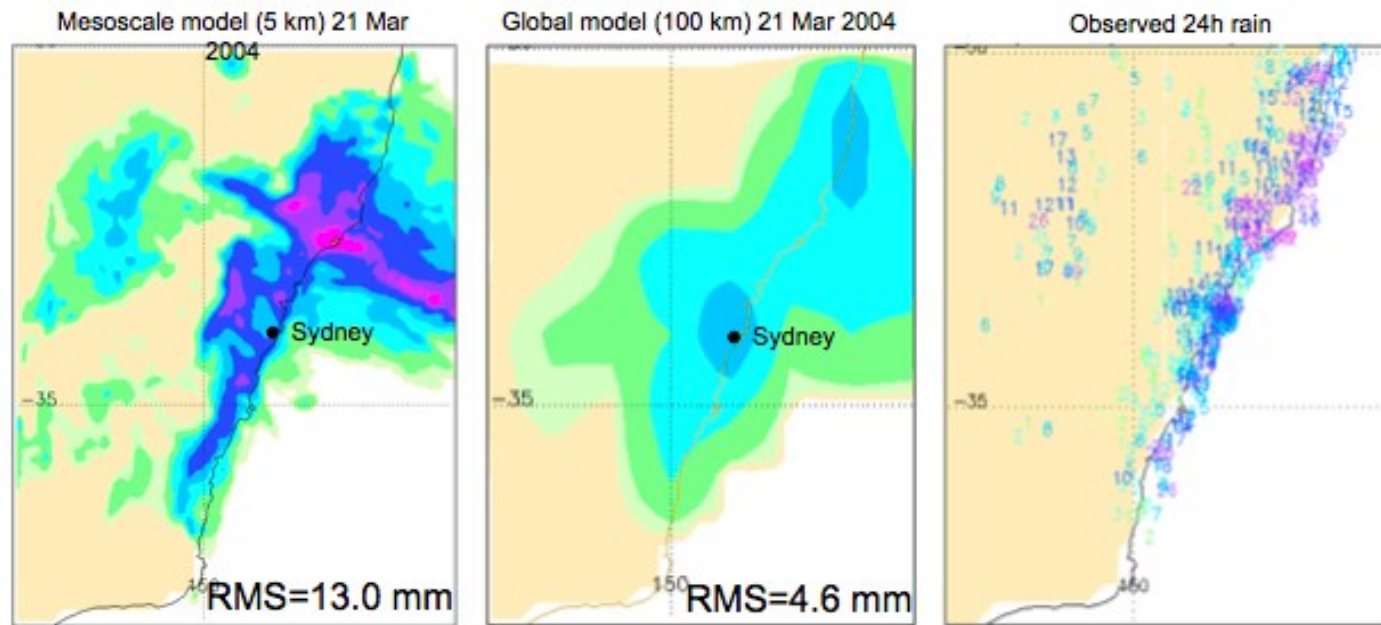
Minneapolis, Minnesota, U.S.A.

National Center for Atmospheric Research



NCAR

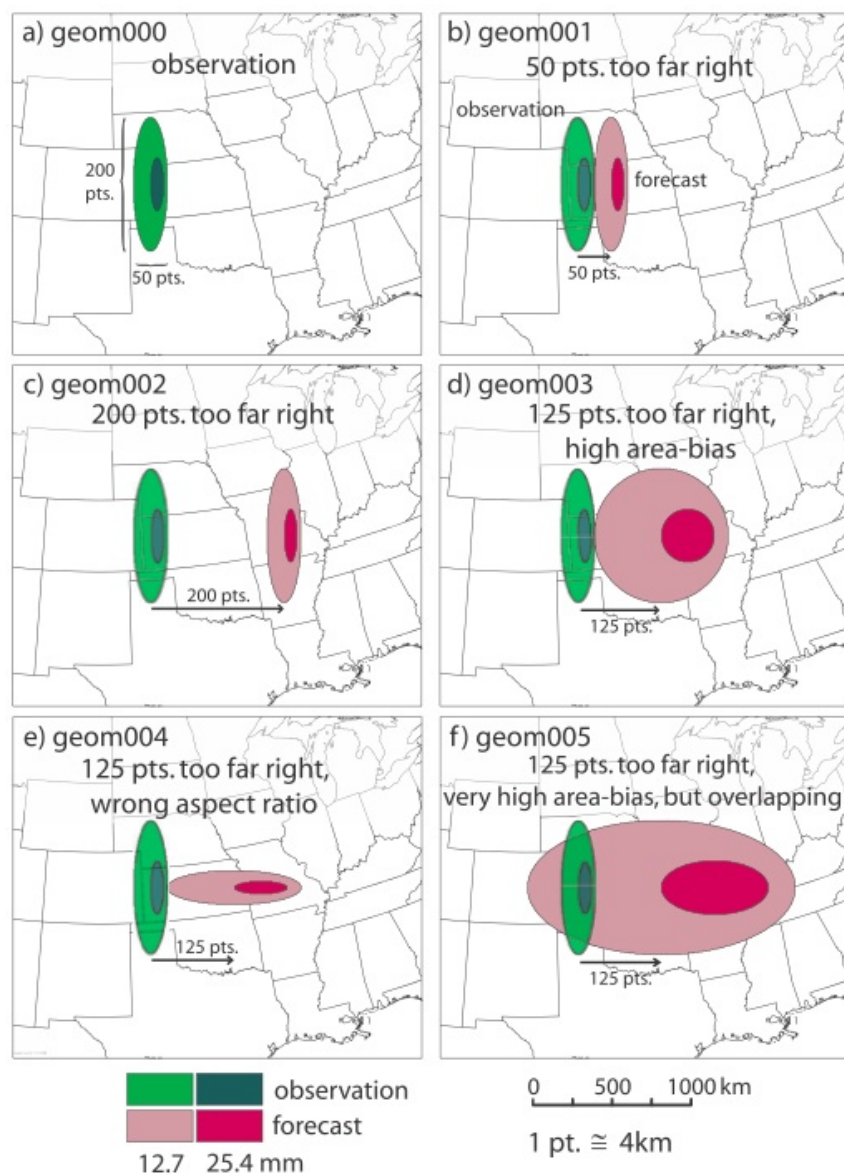
Background



Above Figure from Beth Ebert



Background



Traditional score	geom001/002/004	geom003	geom005
Accuracy	0.95	0.87	0.81
Frequency bias	1.00	4.02	8.03
Multiplicative intensity bias	1.00	4.02	8.04
RMSE (mm)	3.5	5.6	6.9
Bias-corrected RMSE (mm)	3.5	5.5	6.3
Correlation coefficient	-0.02	-0.05	0.20
Probability of detection	0.00	0.00	0.88
Probability of false detection	0.03	0.11	0.19
False alarm ratio	1.00	1.00	0.89
Hanssen-Kuipers discriminant (H-K)	-0.03	-0.11	0.69
Threat score or CSI	0.00	0.00	0.11
Equitable threat score or GSS	-0.01	-0.02	0.08
HSS	-0.03	-0.04	0.16



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Background

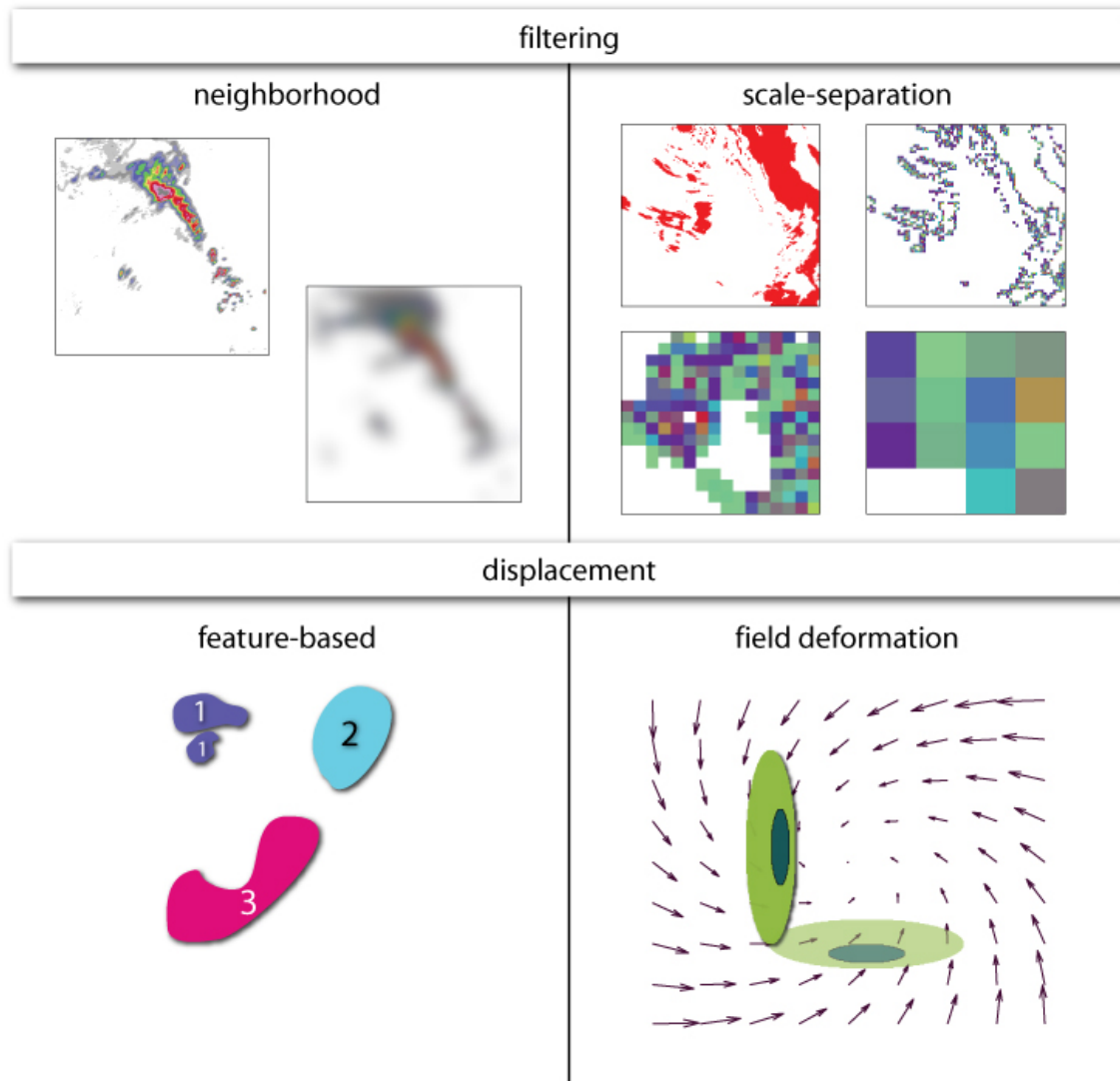


Fig. 2 from G. *et al.* (2010, [10.1175/2010BAMS2819.1](https://doi.org/10.1175/2010BAMS2819.1))

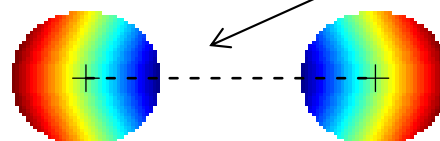


Distance Measures

Pratt's Figure of Merit (FoM) =

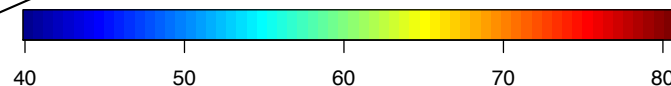
$$\text{FoM}(A,B) = \frac{1}{\max\{n(A), n(B)\}} \sum_{x \in B} \frac{1}{1 + \kappa d(x, A)}$$

centroid distance (CD)



A

B



$$\text{MED}(A, B) = \frac{1}{n(B)} \sum_{x \in B} d(x, A)$$

$n(B)$ is the number of points in the set B.

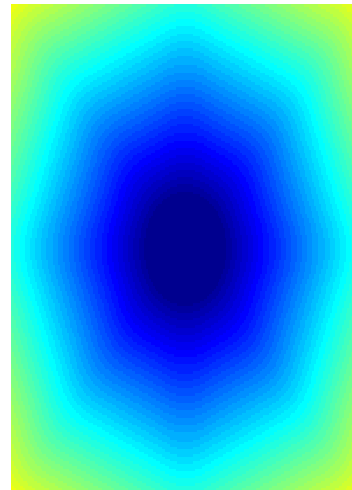
$$\text{MED}(B, A) = \frac{1}{n(A)} \sum_{x \in A} d(x, B)$$

$n(A)$ is the number of points in A.

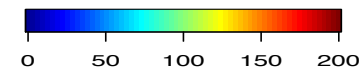
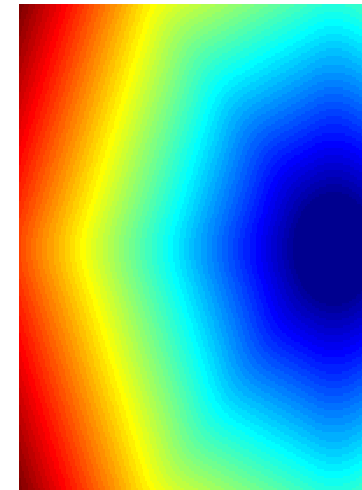


Distance Measures

$d(x, A)$



$d(x, B)$



Distance maps for A and B. Note dependence on location within the domain.

Distance Measures

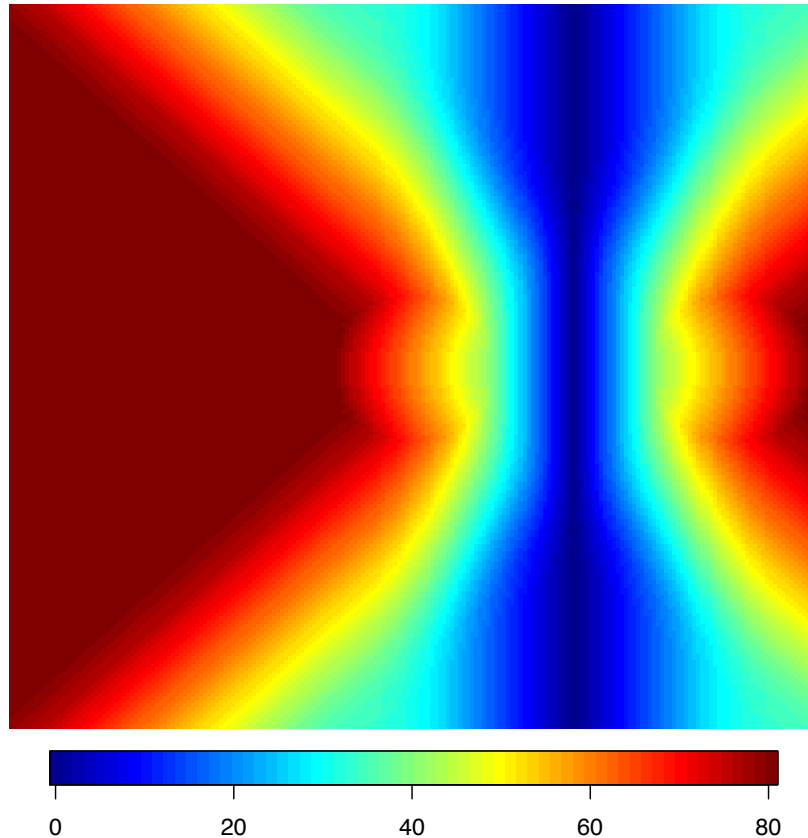


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$$T = |\omega(d(x, A)) - \omega(d(x, B))|$$

Baddeley's Δ Metric

- $p = 1$ gives the arithmetic average of T
- $p = 2$ is the usual choice
- $p = \infty$ gives the max of T (Hausdorff distance, H)



Δ is the L_p norm of T

$d(x, A)$ and $d(x, B)$ are first transformed by a function ω . Usually, $\omega(x) = \max(x, \text{constant})$, but the picture here uses " ∞ " for the constant term.

$$\Delta(B, A) = \Delta(B, A) = \left[\sum_{x \in D} T^p \right]^{1/p} / |N|$$

$|N|$ is the size of the domain, D .



Distance Measures

Zhu's metric (Z) from Zhu et al. (2011, doi: 10.1016/j.atmosres.2011.09.004)

Between forecast F and observation O:

$$Z = \lambda_1 D1 + \lambda_2 D2$$

D1 = root sum of squared differences between the two binary fields (overlap measure)

D2 = MED(F, O) (or MED miss) provided the product of the number of points in either set is not zero. If no 1-valued points are in both F and O. Otherwise, it is set to a large number.

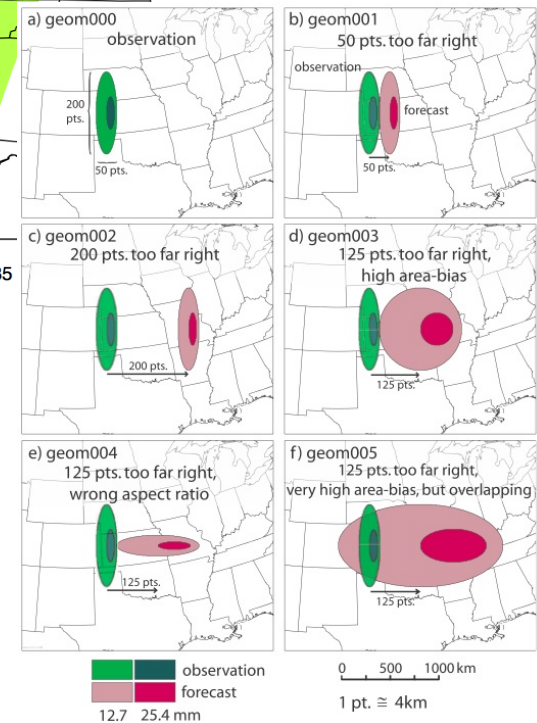
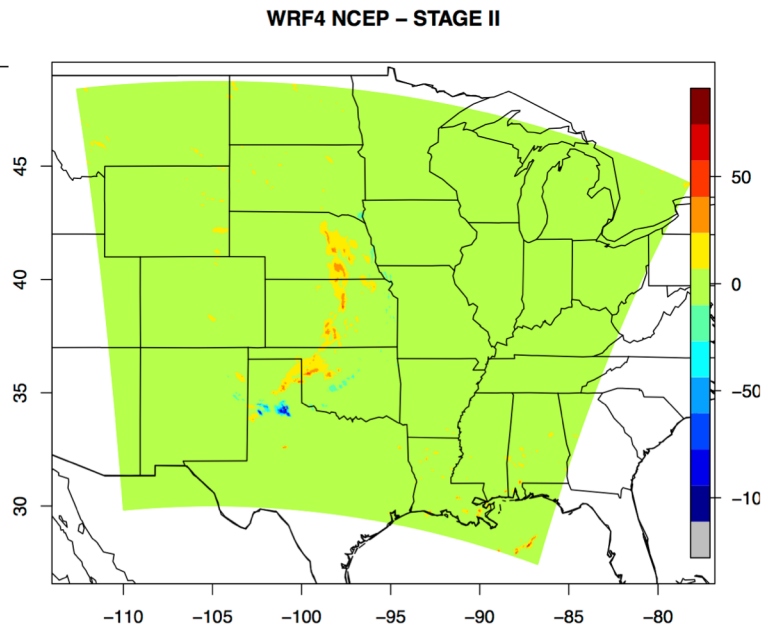
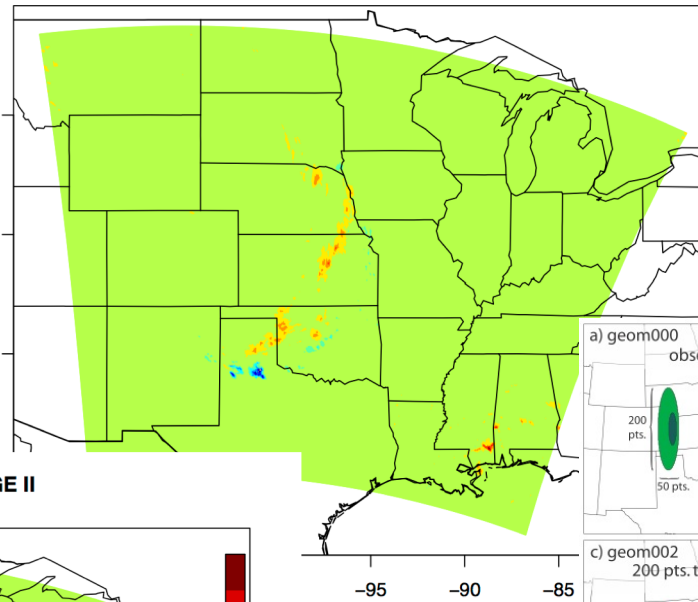
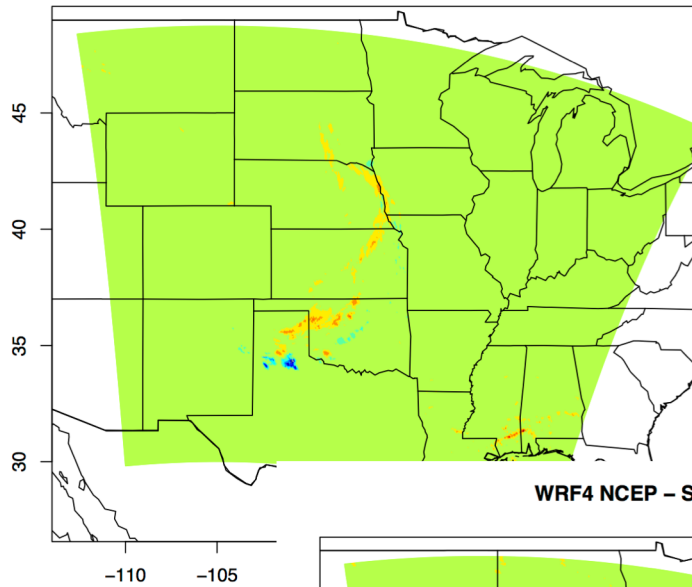
ICP Phase 1



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WRF2 CAPS – STAGE II

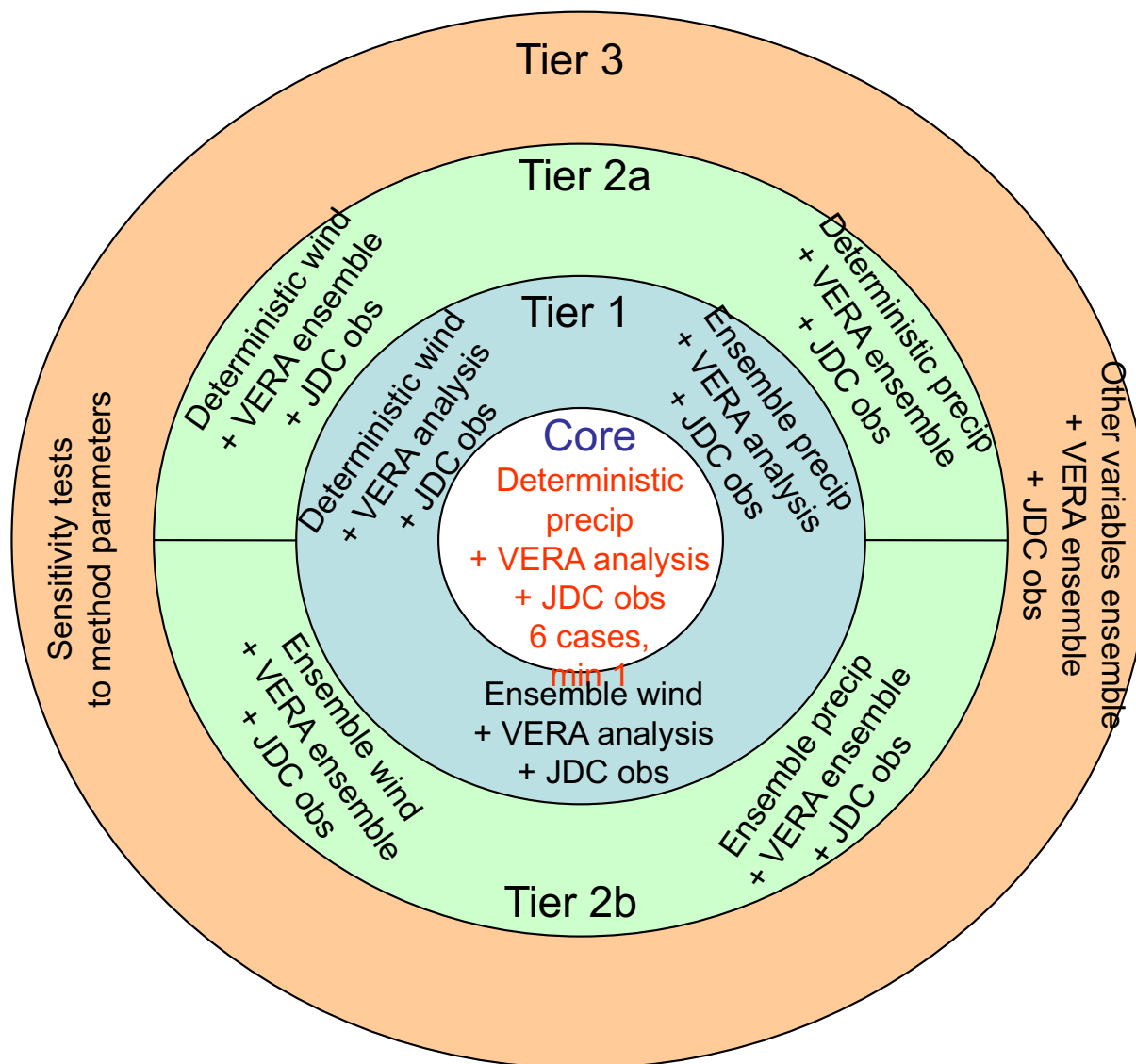
WRF4 NCAR – STAGE II





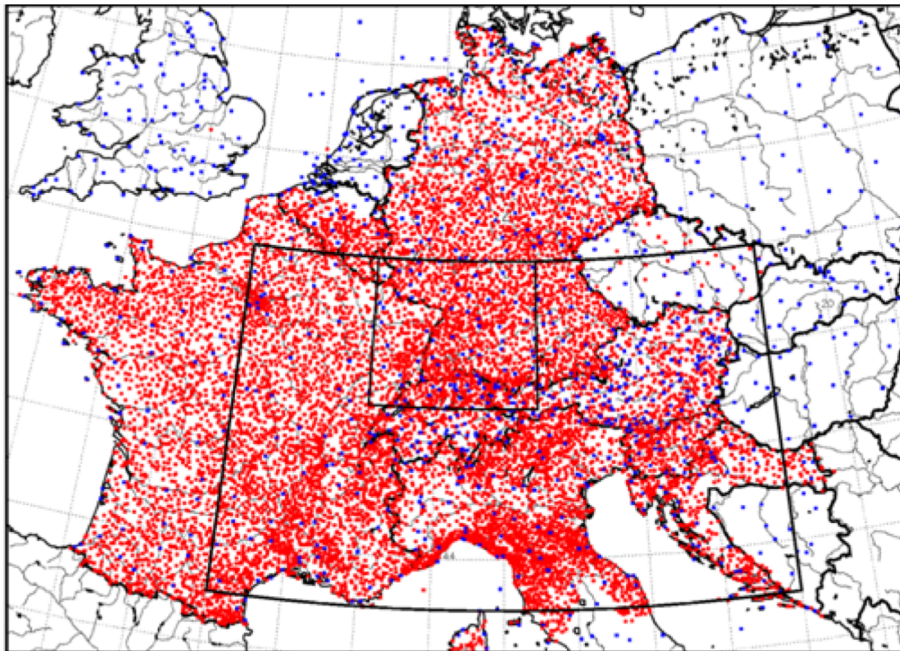
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MesoVICT



MesoVICT

WWRP COPS (RDP, Wulfmeyer, et al., 2008, BAMS) and D-PHASE (FDP, Rotach, et al., 2009, BAMS), data available: (<http://cera-www.dkrz.de/WDCC/ui/Index.jsp>)



Observations-Joint D-PHASE COPS (JDC) data-set

- 32 data providers
- GTS-Stations: 1232
- NGTS-Stations: > 13000
- Mean station distance: GTS: ~ 36km
GTS+Non-GTS: ~ 12km

Frames: D-PHASE (large)
& COPS (small) areas

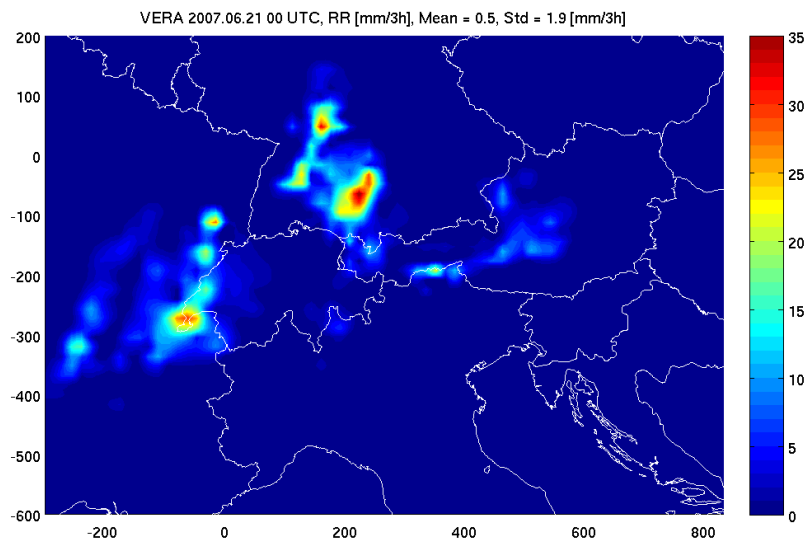


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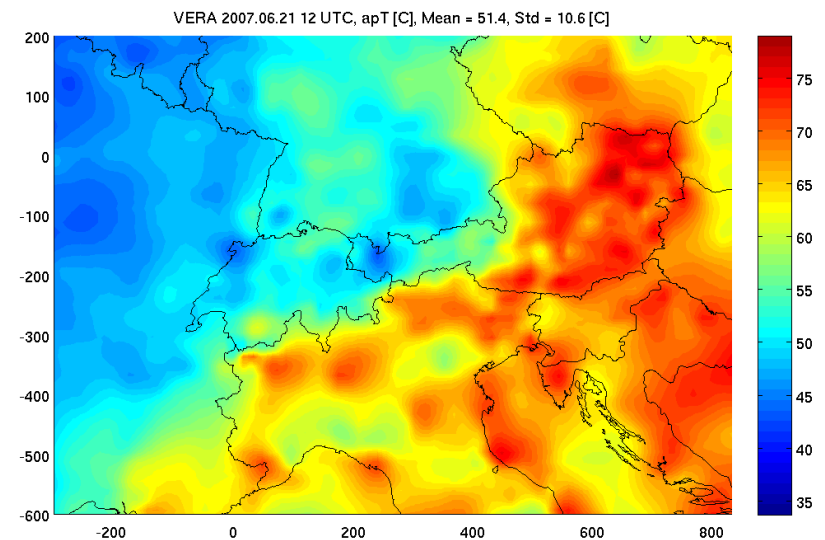
MesoVICT

Case 1 (**core case**): 20-22 June 2007 (COPS IOP case)

Strong convective developments north of the Alps followed by a cold front the next day. Cold air mass could not spill over the Alps.



Precipitation analysis for the 3h-period ending at 21 June 2007, 00 UTC.



Equivalent potential temperature analysis for 21 June 2007, 12 UTC.

New Geometric Cases



Pathological Cases

P1: Null Case

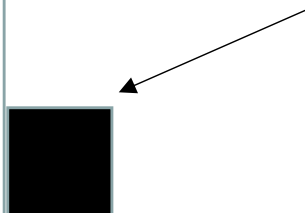
P2: Full Case



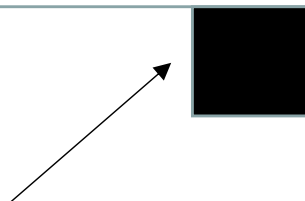
New Geometric Cases

Pathological Cases

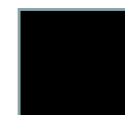
P3: Exactly one grid cell with value 1 and all else are zero.



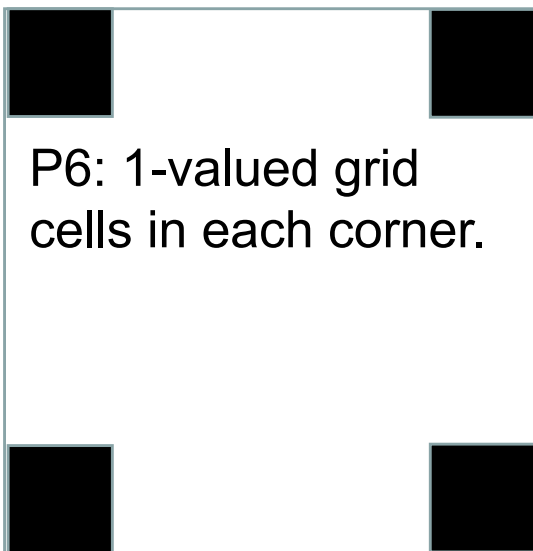
P4: Same as P5, but upper right corner instead of lower left.



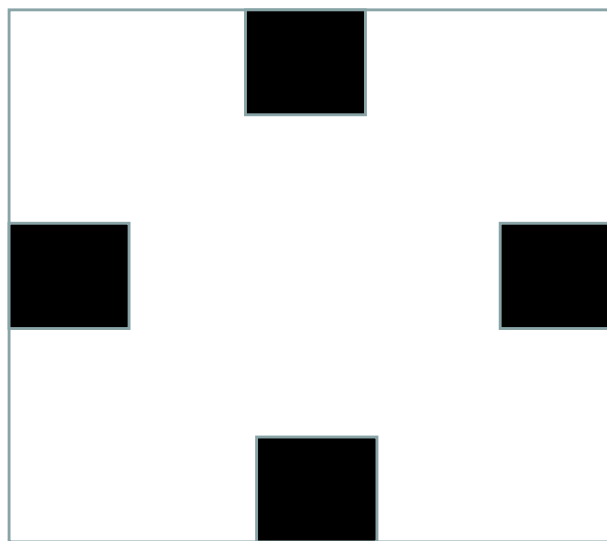
P5: Same as P3 and P4, but in center of grid.



P6: 1-valued grid cells in each corner.



P7: Four 1-valued grid cells located on boundaries midway between corners





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New Geometric Cases

$\Delta = \mathcal{D} = H = CD = MED = Z = 0.00$, FoM undefined

FoM(P2, P1) undefined
MED(P2, P1) undefined

P1P1: Perfect null (all errors = 0)

P1P2: Perfectly bad (all errors = -1)

$\Delta = H = 400.00$
 $\mathcal{D} = 401.99$
 $CD = 142.13$
 $Z = 200$

rP1P2: Perfectly bad (all errors = 1)

P2P2: Perfect full (all errors = 0)

F – O

FoM(P1, P2) = 0.00
MED(P1, P2) = 400.00

$\Delta = \mathcal{D} = H = CD = MED = Z = 0.00$, FoM = 1.00



New Geometric Cases

P1P3: Exactly one grid cell with error = -1 and all else are zero.

$\Delta = 246.29$
 $\bar{D} = 322.12$, $H = 400.00$
 $CD = 1.41$, $Z = 100.50$

FoM(P1, P3) = 0.00
 MED(P1, P3) = 400.00

rP1P3: Exactly one grid cell with error = 1 and all else are zero.

FoM(P3, P1) undefined
 MED(P3, P1) undefined

P1P4: Same as P1P3, but different placement of the error.

$\Delta = 246.29$
 $\bar{D} = 322.12$, $H = 400.00$
 $CD = \mathbf{282.84}$, $Z = 100.50$

P1P5: Same as P1P3 and P1P4, but different placement of the error.

$\Delta = \mathbf{320.51}$
 $\bar{D} = 322.12$, $H = 400.00$
 $CD = \mathbf{141.42}$, $Z = 100.50$

FoM(P1, P5) = 0.00
 MED(P1, P5) = 400.00
 MED(P5, P1) undefined

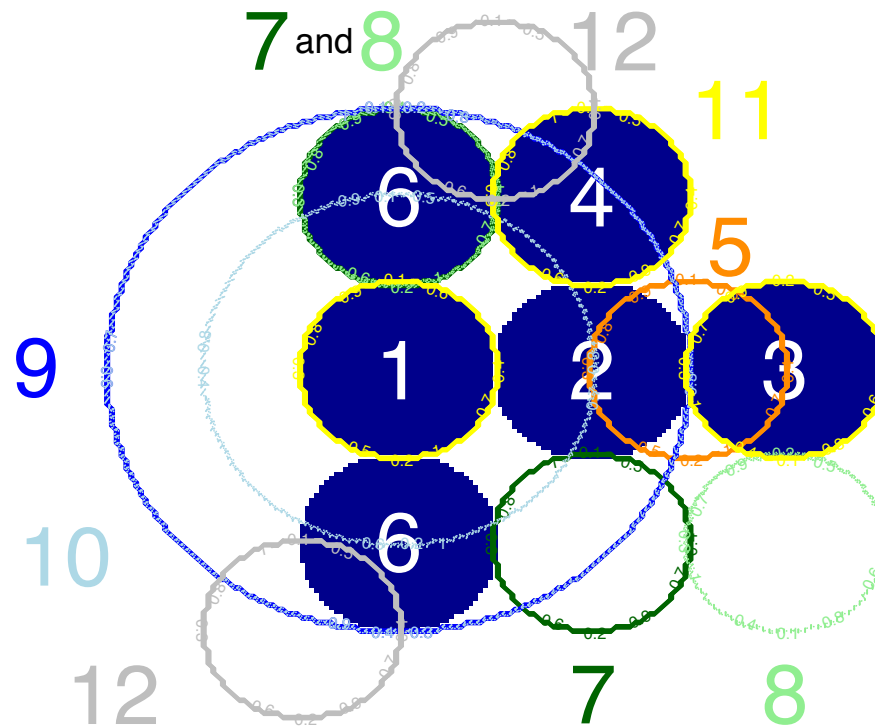
P2P5: Same as P1P5 but the one grid square is the only non-error.

$\Delta = 86.21$
 $\bar{D} = 86.62$, $H = 142..13$
 $CD = 0.71$, $Z = 140.44$
 FoM(P2, P5) = 0.01
 MED(P2, P5) = 0.00, MED(P5, P2) = 80.88

FoM(P1, P4) = 0.00
 MED(P1, P4) = 400.00
 MED(P4, P1) undefined

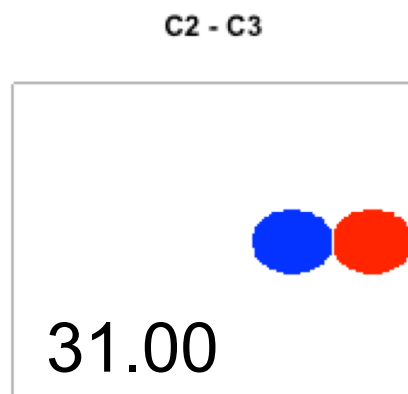
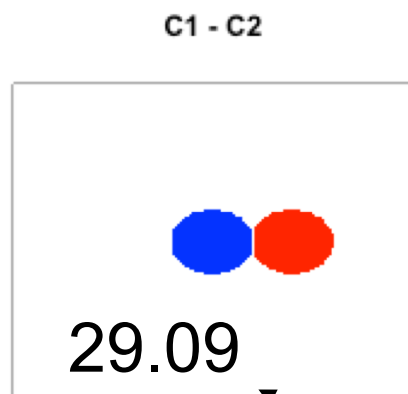
F – O

New Geometric Cases

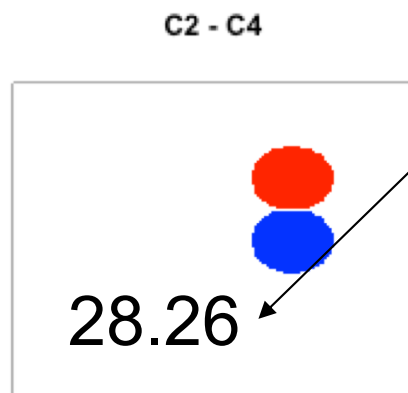


Circle Cases

New Geometric Cases



F - O



Baddeley's Δ

$$\mathfrak{D} = 28.84$$

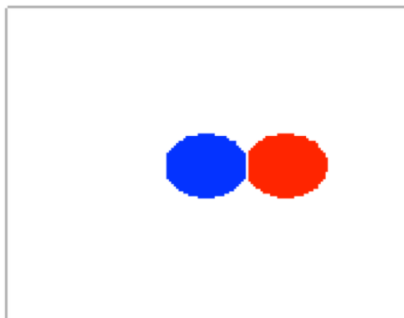
$$\text{Hausdorff} = 40.20$$

$$\text{Centroid distance} = 40.00$$

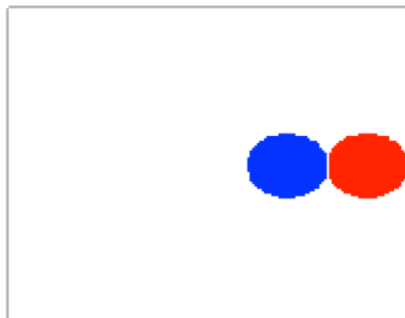
$$\text{Zhu's metric} = 36.81$$

New Geometric Cases

C1 - C2

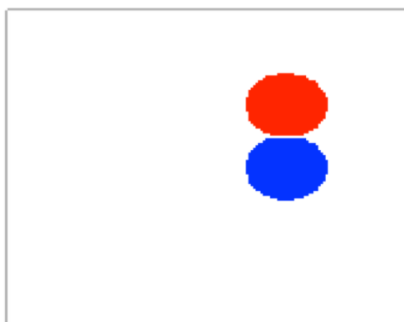


C2 - C3



F - O

C2 - C4



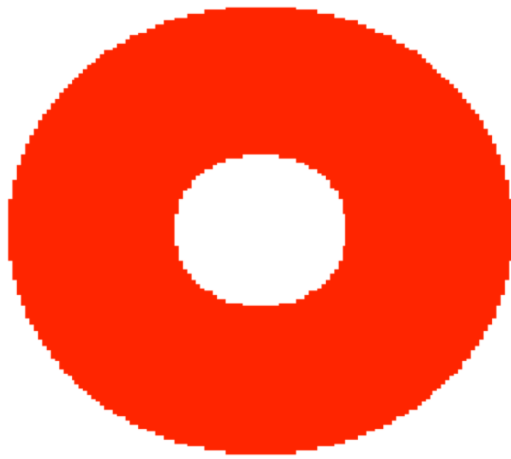
$MED(\text{False Alarm}) = MED(\text{Miss}) = 21.92$
 $FoM(\text{False Alarm}) = FoM(\text{Miss}) = 0.07$



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New Geometric Cases

C1 - C9



$C1 \subset C9$

$F - O = C1 - C9$

Baddeley's $\Delta = 38.13$

$\bar{D} = 38.17$

Hausdorff = 43.43

Centroid distance = 0.00

Zhu's metric = 50.5

MED(Miss) = 21.72

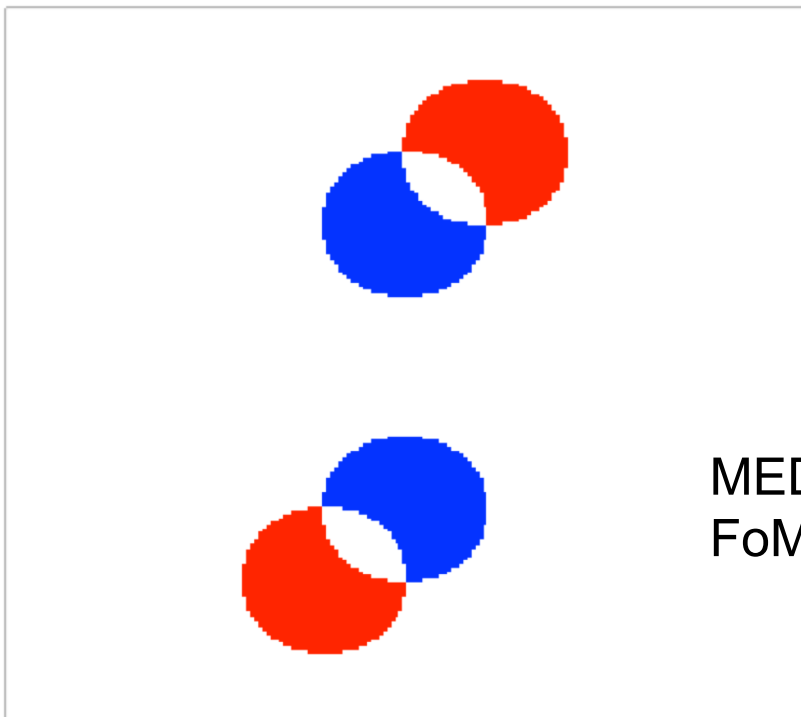
MED(False Alarm) = 0.00

FoM(Miss) = 0.12

FoM(False Alarm) = 0.18

New Geometric Cases

C6 - C12



$$\Delta = 18.84$$

$$\bar{D} = 18.85$$

$$H = 28.43$$

$$CD = 0.00$$

$$Z = 38.36$$

$$\text{MED}(\text{Miss}) = \text{MED}(\text{False Alarm}) = 11.24$$

$$\text{FoM}(\text{Miss}) = \text{FoM}(\text{False Alarm}) = 0.32$$

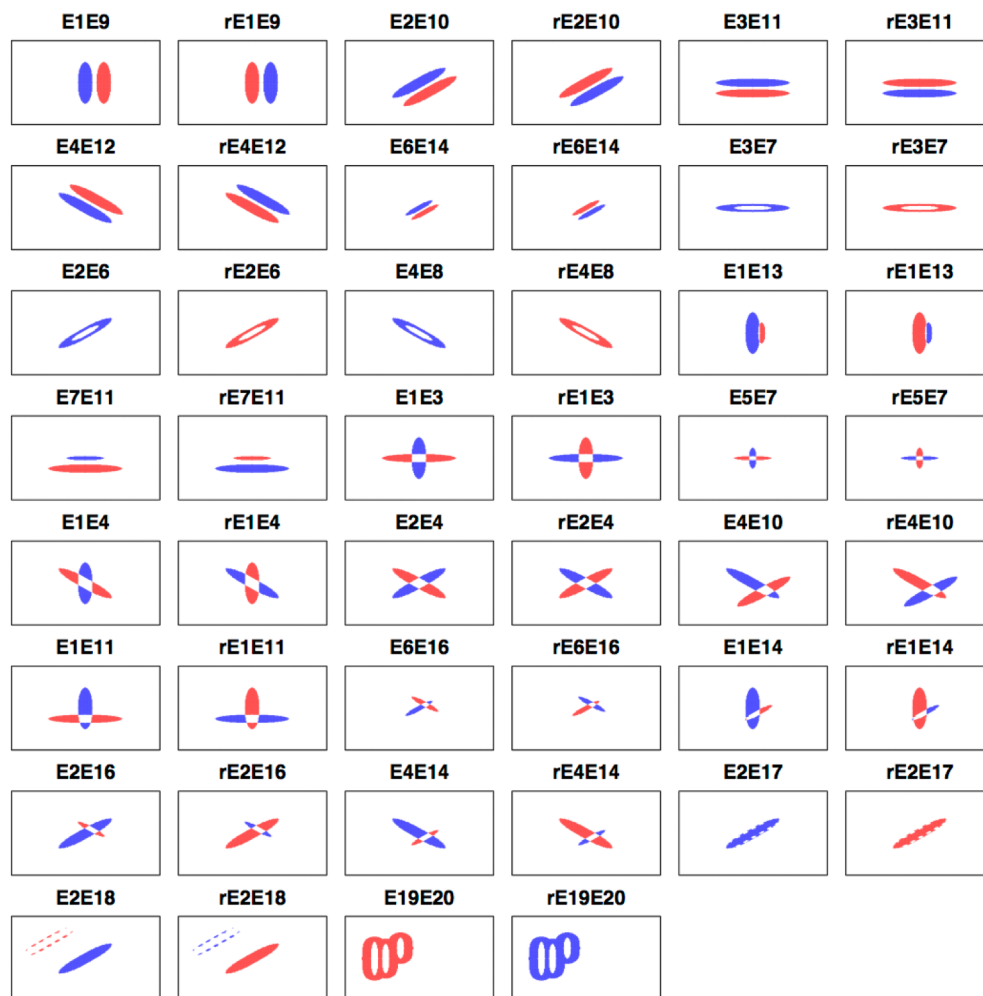
$$F - O = C6 - C12$$



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New Geometric Cases

Complex Terrain
Cases



New Geometric Cases



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$\Delta = 22.53$
 $\bar{D} = 22.52$, $H = 25.13$
 $CD = 25.00$, $Z = 36.41$

E1E9



FoM = 0.05
 MED = 17.09

$\Delta = 14.15$
 $\bar{D} = 14.18$, $H = 25.13$
 $CD = 0.00$, $Z = 20.02$

E3E7



FoM(Miss) = 0.5
 FoM(False Alarm) = 0.25
 MED(Miss) = 0.00
 MED(False Alarm) = 5.86

$\Delta = 17.98$
 $\bar{D} = 17.84$, $H = 40.2$
 $CD = 12.00$, $Z = 27.16$

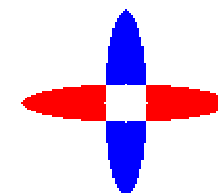
E1E13



FoM(Miss) = 0.19
 FoM(False Alarm) = 0.14
 MED(Miss) = 3.10
 MED(False Alarm) = 12.01

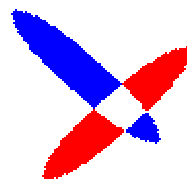
$\Delta = 23.51$
 $\bar{D} = 23.53$, $H = 40.2$
 $CD = 0.00$, $Z = 27.16$

E1E3



FoM = 0.34
 MED = 13.30

E4E10

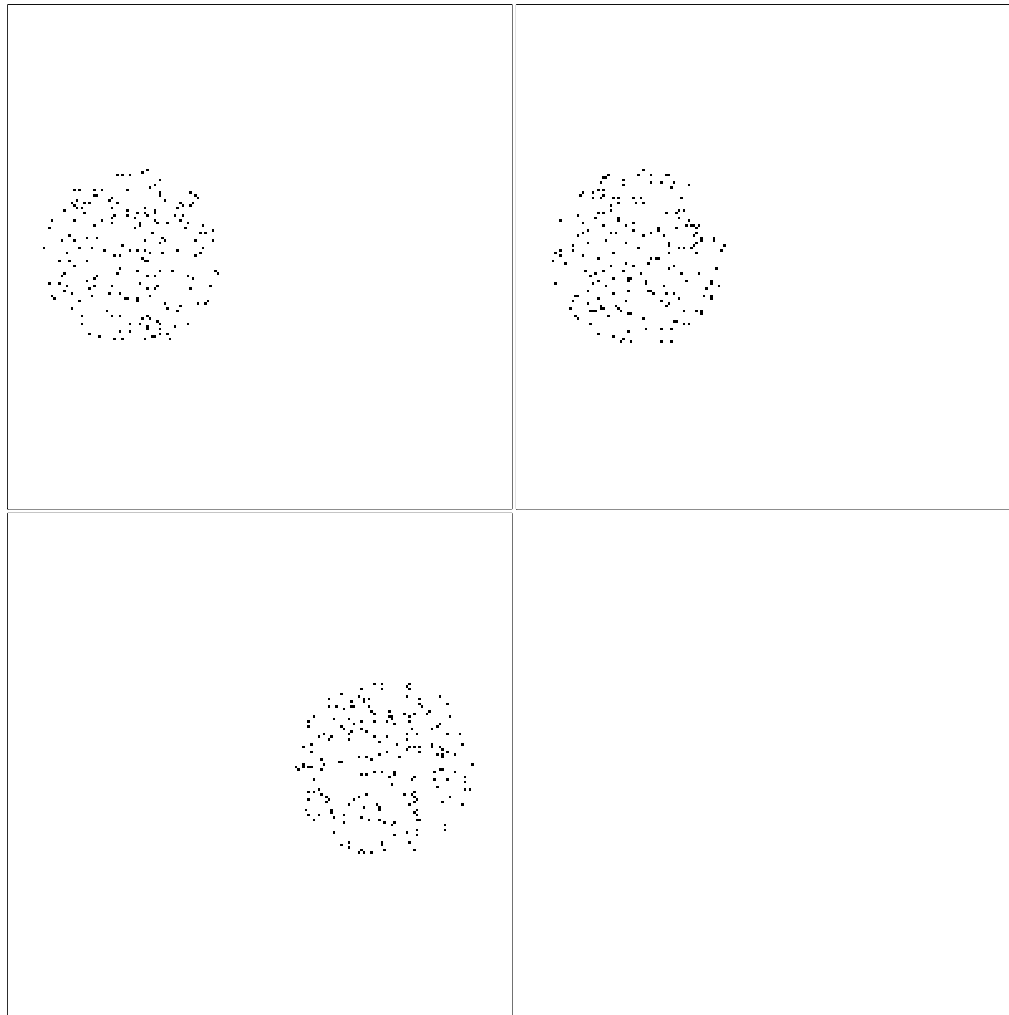


$\Delta = 32.16$
 $\bar{D} = 31.18$, $H = 65.38$
 $CD = 25.00$, $Z = 35.23$

FoM(Miss) = 0.32
 FoM(False Alarm) = 0.30
 MED(Miss) = 14.08
 MED(False Alarm) = 20.76

F – O

New Geometric Cases

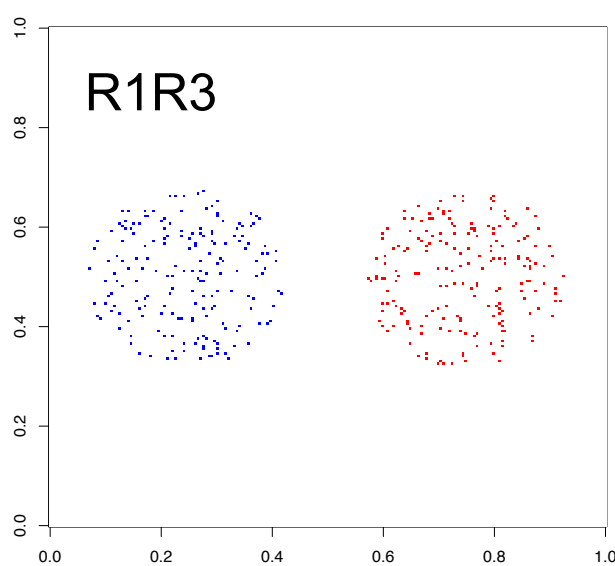
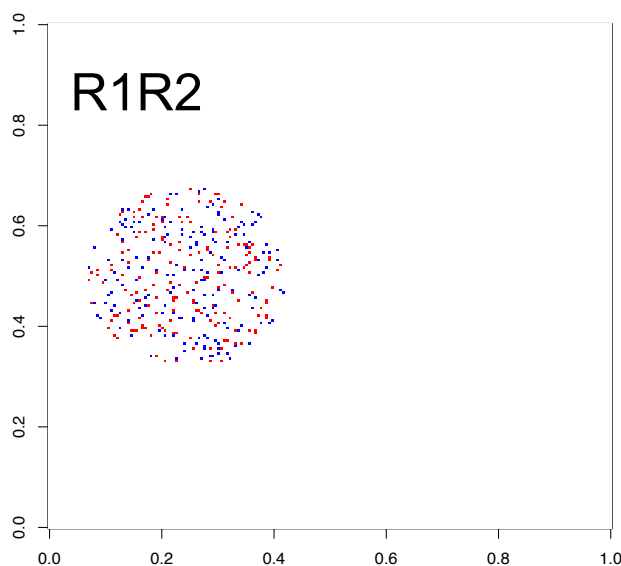


Random Rain Cases

New Geometric Cases

$\Delta = 1.91$
 $\bar{D} = 1.78, H = 9.12$
 $CD = 1.30, Z = 10.59$
 $FoM = 0.62$
 $MED(\text{False Alarm}) = 2.37$
 $MED(\text{Miss}) = 2.56$

Random Rain Cases



$\Delta = 63.39$
 $\bar{D} = 63.49, H = 104.42$
 $CD = 99.11, Z = 45.06$
 $FoM = 0.00$
 $MED(\text{False Alarm}) = 70.04$
 $MED(\text{Miss}) = 70.60$

New Geometric Cases

Additional Cases include:

- Holes (inverted C1 and C2)
- C1C4 with noise added
- C1C4 with P3 added
- C1C4 with P5 added



Summary

- Overview paper of project accepted to BAMS (available at Early online release: <https://journals.ametsoc.org/doi/pdf/10.1175/BAMS-D-17-0164.1>).
- Special Collection of Papers for Monthly Weather Review
- SpatialVx (R package for performing many of the spatial methods; still in beta form—use at your own risk!)
- All test cases and other information (including preliminary results) available at MesoVICT web site (<https://ral.ucar.edu/projects/icp/>)
- New geometric cases available soon (paper in progress).

Thank you



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<https://ral.ucar.edu/staff/ericg/>